

G2C3

Global Gyrokinetic

Code using Cylindrical Coordinates



Neural network-assisted electrostatic global gyrokinetic toroidal code using cylindrical coordinates

Jaya Kumar A¹, Joydeep Das¹, Sarveshwar Sharma², Abhijit Sen^{2,3}, Animesh Kuley¹

¹Department of Physics, Indian Institute of Science, Bangalore

²Institute for Plasma Research, Bhat, Gandhinagar

³Homi Bhabha National Institute, Anushaktinagar, Mumbai



Apr 3, 2024

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Global Gyrokinetic

Code using Cylindrical Coordinates



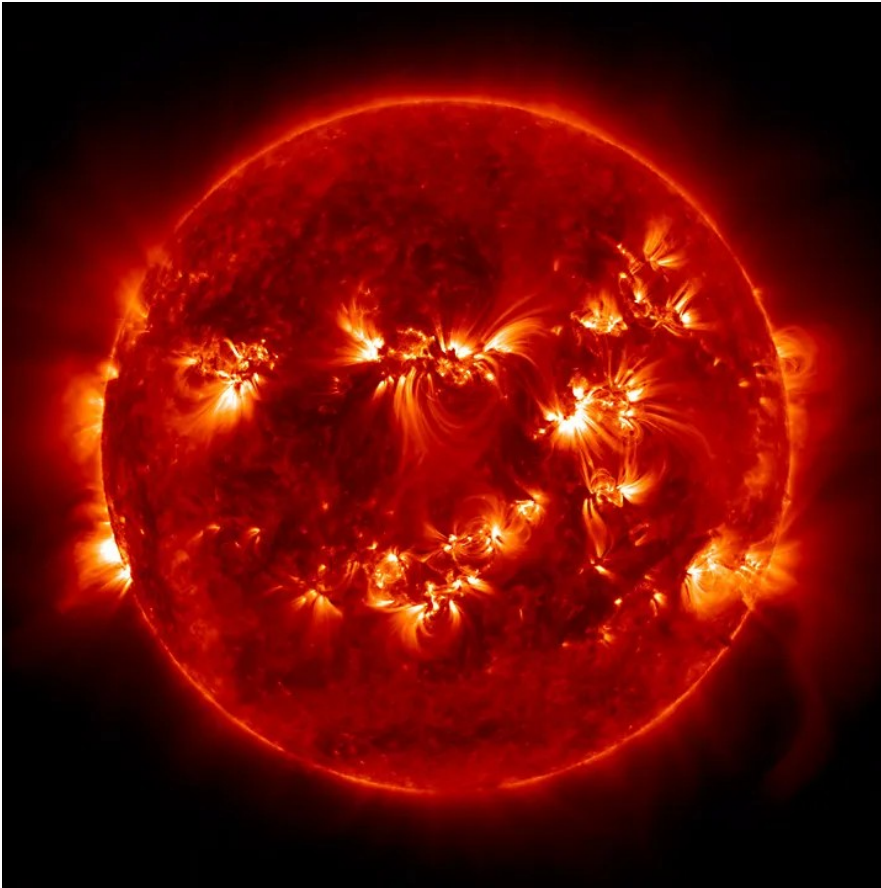
Neural network-assisted electrostatic global gyrokinetic toroidal code using cylindrical coordinates

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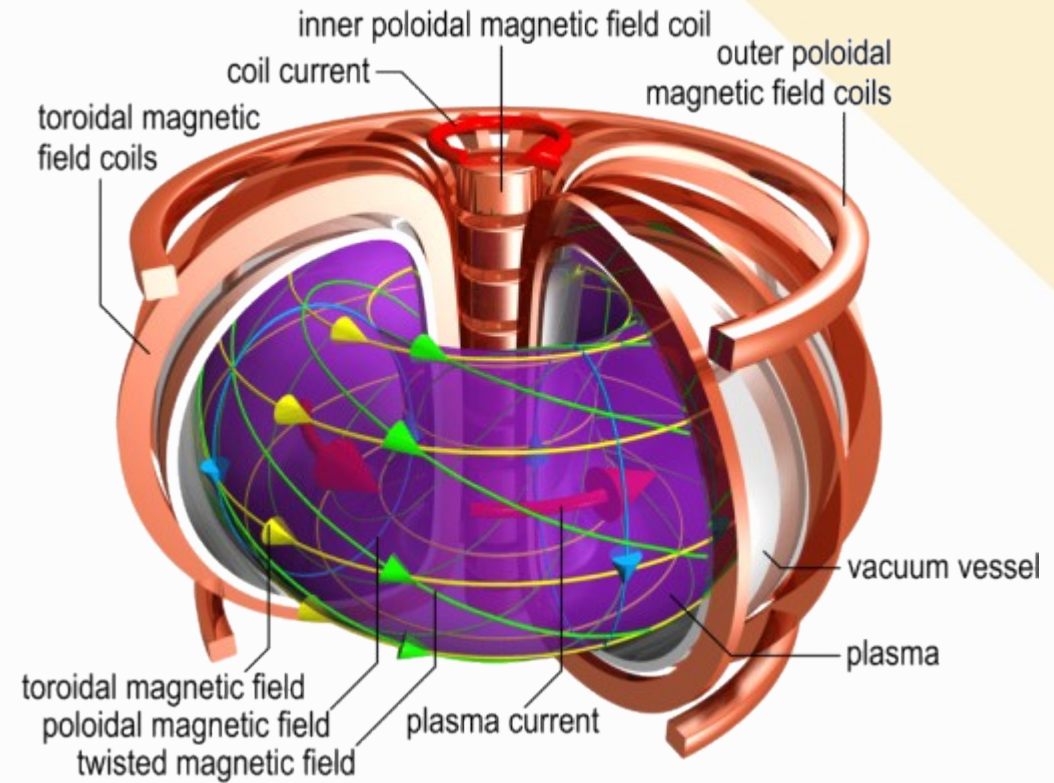
Apr 3, 2024

Nuclear Fusion Reactor



The only working nuclear fusion reactor in our solar system!

*Earth-orbiting Solar Dynamics Observatory (2015)



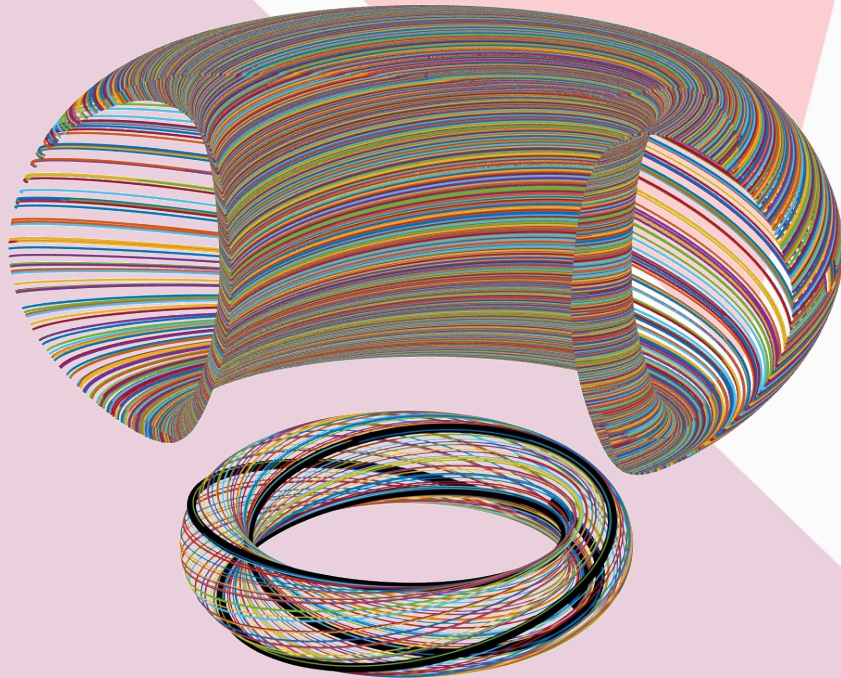
*J. H. E. Proll, Trapped-particle instabilities in quasi-isodynamic stellarators

Tokamak
“Sun in a magnetic bottle”



Importance and objective

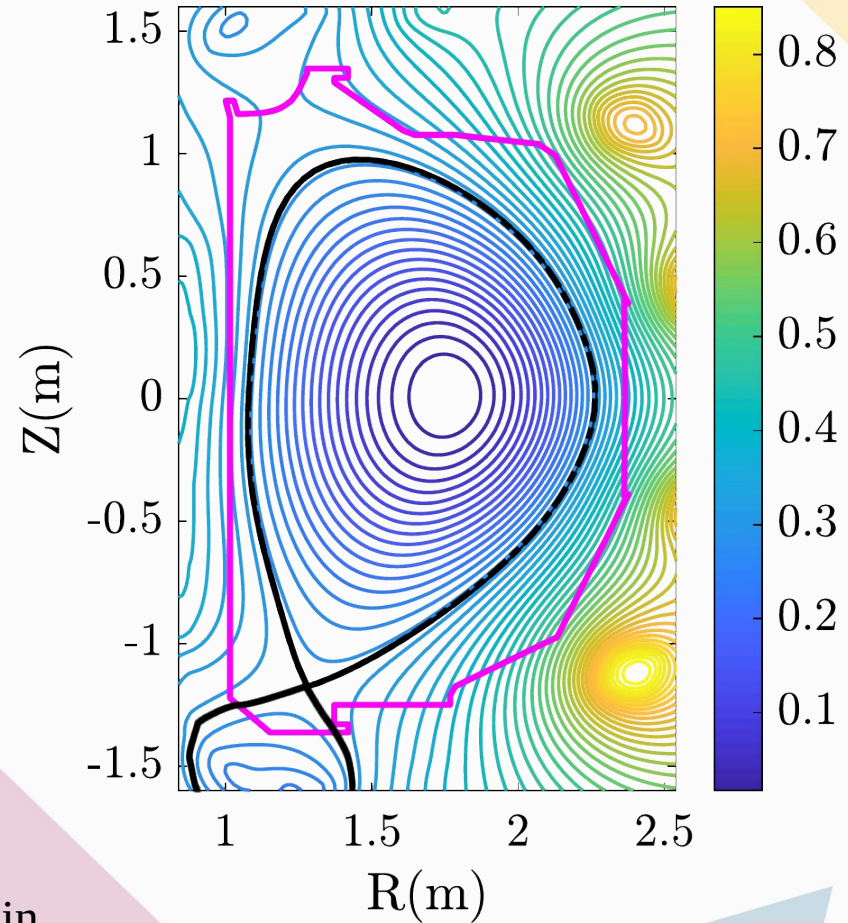
Magnetic field lines on a flux surface



Explore the physics of microturbulent transport in the open flux surface region of tokamak (DIII-D, ADITYA-U).

G2C3

DIII-D shot # 158103

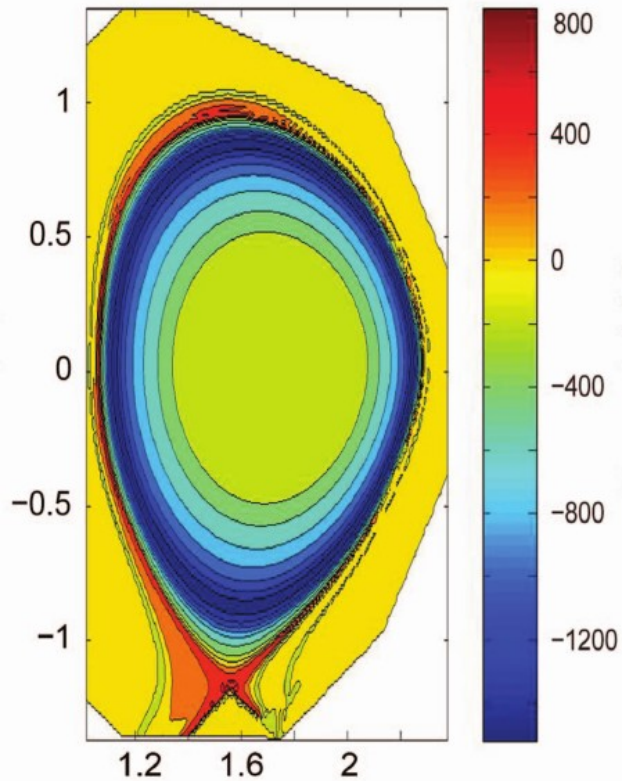


Magnetic flux surface

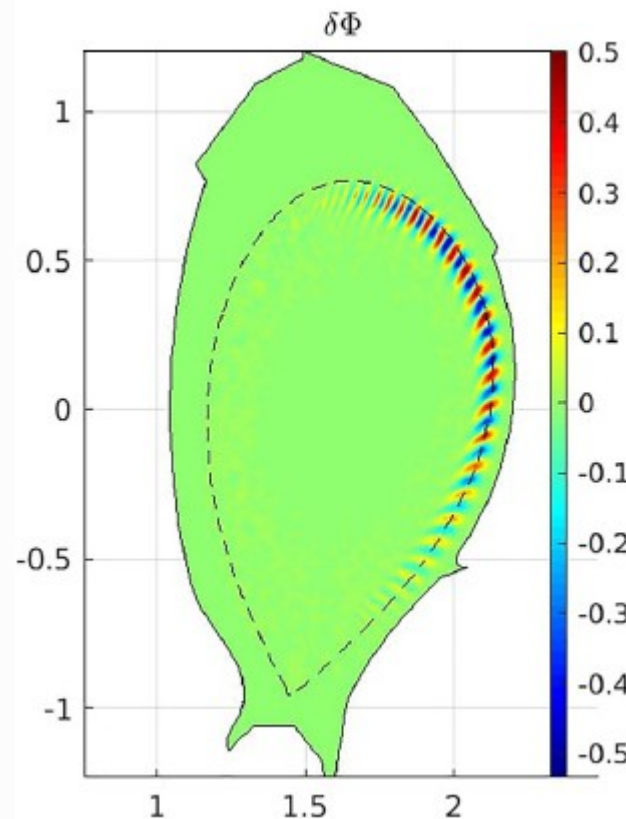
Codes available:

XGC (PPPL, USA), GENE-X,
TRIMEG (Max-Planck, Germany)

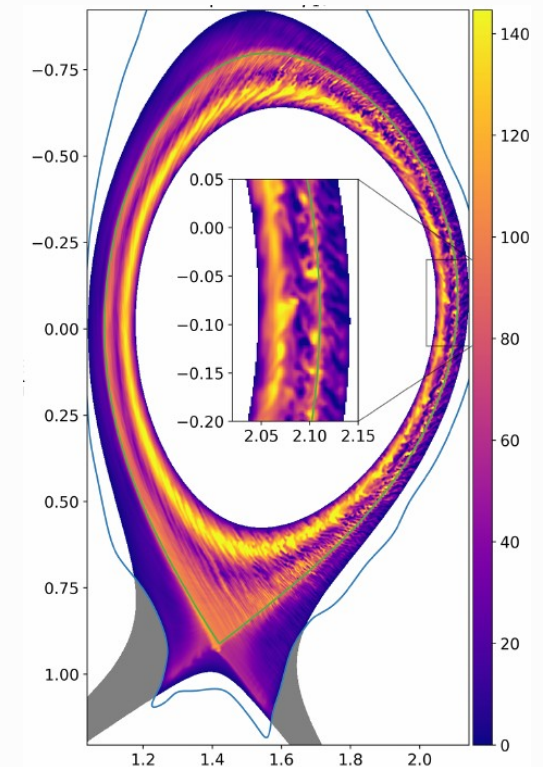
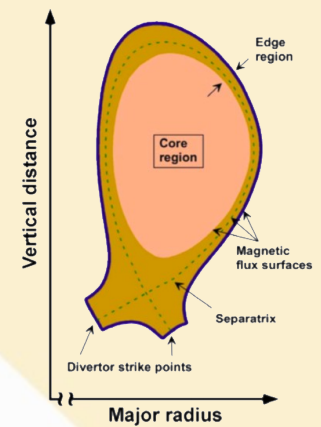
Importance and objective



(XGC) C. S. Chang; S. Ku
Phys. Plasmas 15, 062510 (2008)



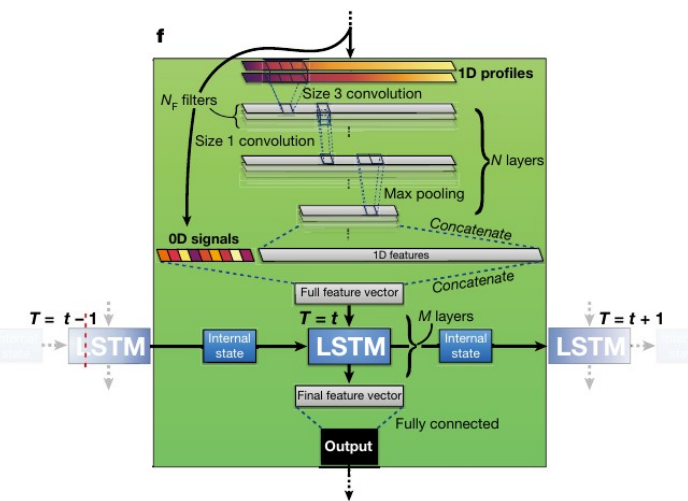
(TRIMEG) Z.X. Lu, et.al.
Plasmas 26, 122503 (2019)



(GENE-X) D. Michels, et.al.
Phys. Plasmas 29, 032307 (2022)

Electrostatic potential

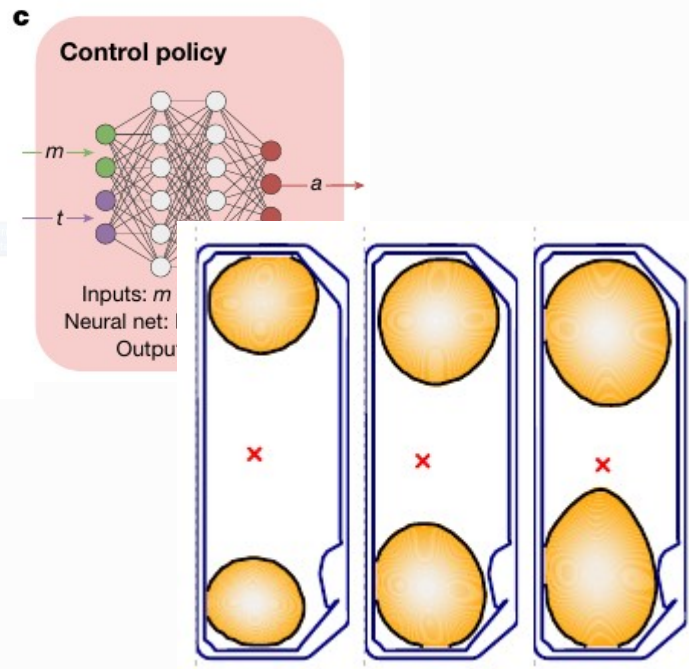
ML in tokamak nuclear fusion research



(DIII-D/JET) J.K. Harbeck, et.al.
Nature, Vol 568, Apr 2019

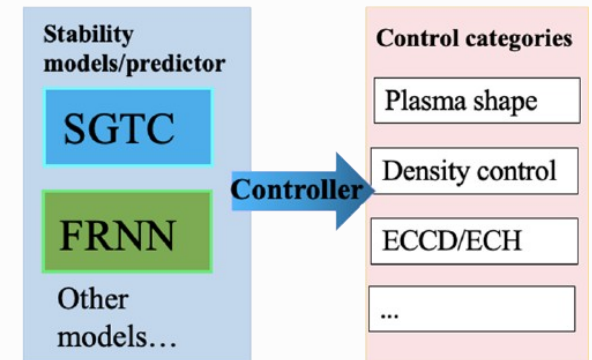
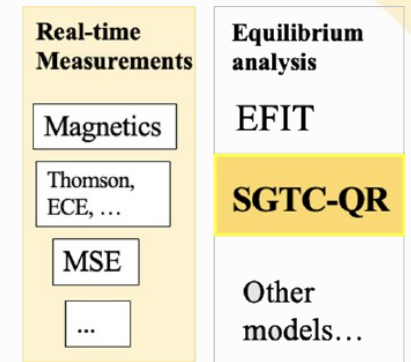
Disruption-prediction

Experimental data-driven



(TCV) J. Degraeve, et.al.
Nature, Vol 602, Feb 2022

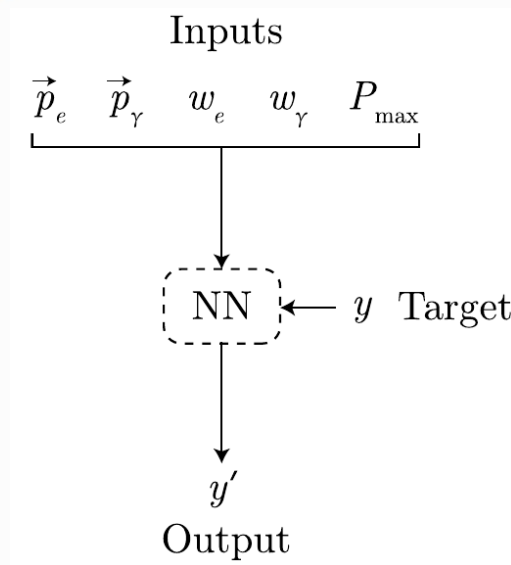
Shape control



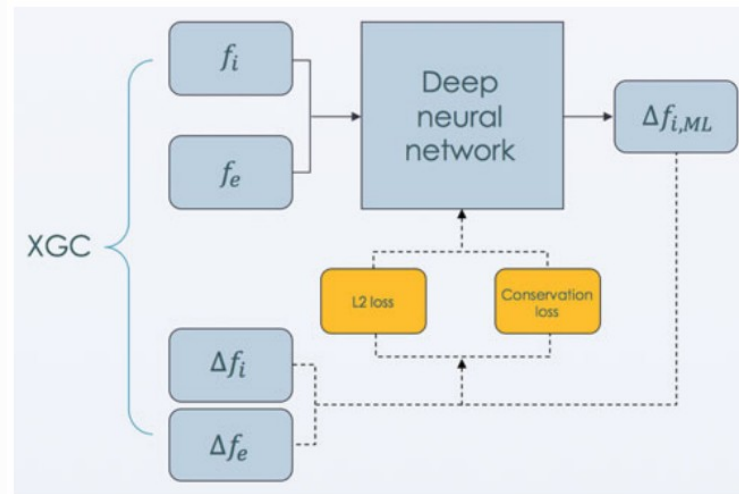
(DIII-D) X. Wei, et.al.
Nucl. Fusion 63, 2023

Profile reconstruction

ML in plasma simulations

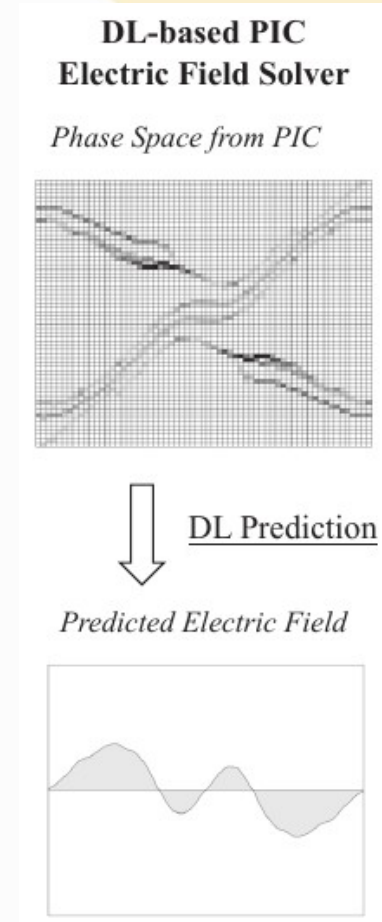


(OSIRIS) C.Badiali, et.al.
J. Plasma Phys. (2022), vol. 88



(XGC) M.A. Miller, et.al.
J. Plasma Phys. (2021), vol. 87

**ML-based
Collision operator**



(PIC) X. Aguilar, et.al.
IEEE International Conference
on Cluster Computing, (2021)

**ML-based
Electric solver**

Simulation data-driven

**Reduced/Surrogate
model**

The Vlasov–Maxwell system of equations

$$\frac{\partial f_e}{\partial t} + \mathbf{v}_e \cdot \nabla f_e - e \left(\mathbf{E} + \frac{\mathbf{v}_e}{c} \times \mathbf{B} \right) \cdot \frac{\partial f_e}{\partial \mathbf{p}} = 0$$
$$\frac{\partial f_i}{\partial t} + \mathbf{v}_i \cdot \nabla f_i + Z_i e \left(\mathbf{E} + \frac{\mathbf{v}_i}{c} \times \mathbf{B} \right) \cdot \frac{\partial f_i}{\partial \mathbf{p}} = 0$$

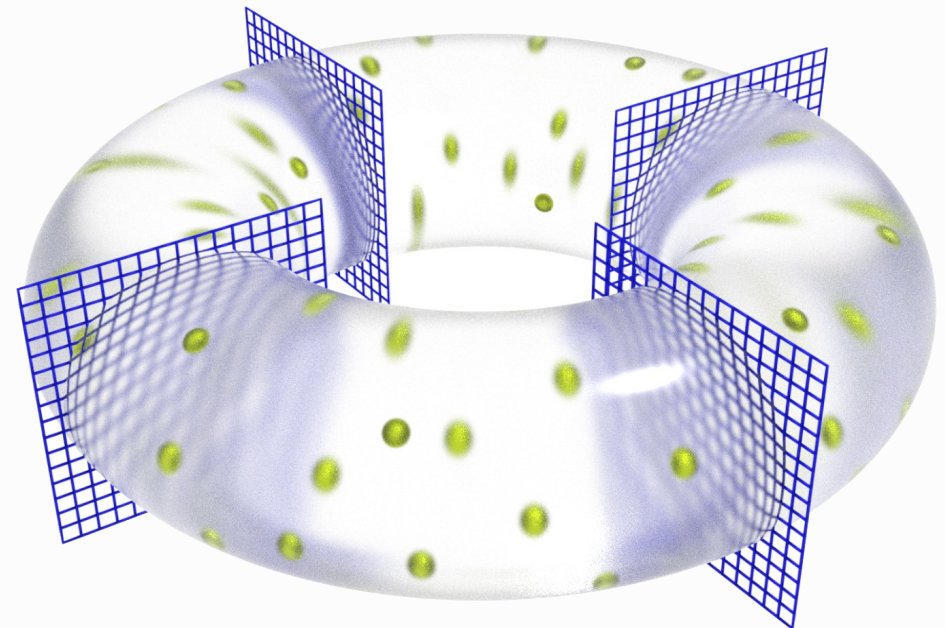
$$\nabla \times \mathbf{B} = \frac{4\pi \mathbf{j}}{c} + \frac{1}{c} \frac{\partial \mathbf{E}}{\partial t}$$

$$\nabla \times \mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \cdot \mathbf{E} = 4\pi \rho$$

$$\nabla \cdot \mathbf{B} = 0$$

Particle-in-cell



Collisionless Kinetic theory

The Vlasov–Maxwell system of equations

$$\frac{\partial f_e}{\partial t} + \mathbf{v}_e \cdot \nabla f_e - e \left(\mathbf{E} + \frac{\mathbf{v}_e}{c} \times \mathbf{B} \right) \cdot \frac{\partial f_e}{\partial \mathbf{p}} = 0$$

$$\frac{\partial f_i}{\partial t} + \mathbf{v}_i \cdot \nabla f_i + Z_i e \left(\mathbf{E} + \frac{\mathbf{v}_i}{c} \times \mathbf{B} \right) \cdot \frac{\partial f_i}{\partial \mathbf{p}} = 0$$

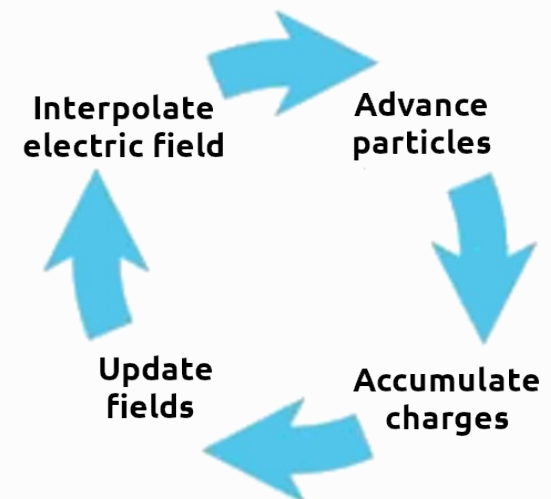
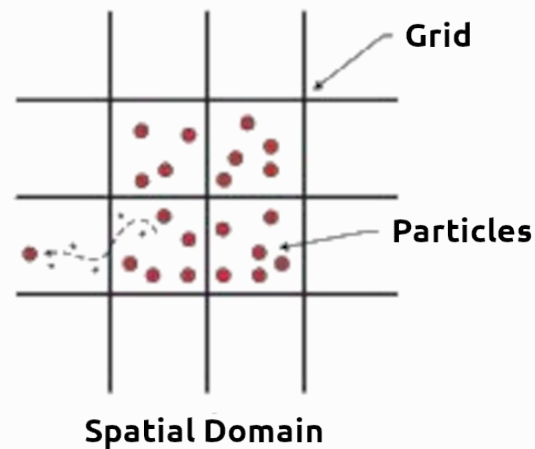
$$\nabla \times \mathbf{B} = \frac{4\pi \mathbf{j}}{c} + \frac{1}{c} \frac{\partial \mathbf{E}}{\partial t}$$

$$\nabla \times \mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \cdot \mathbf{E} = 4\pi \rho$$

$$\nabla \cdot \mathbf{B} = 0$$

Particle-in-cell

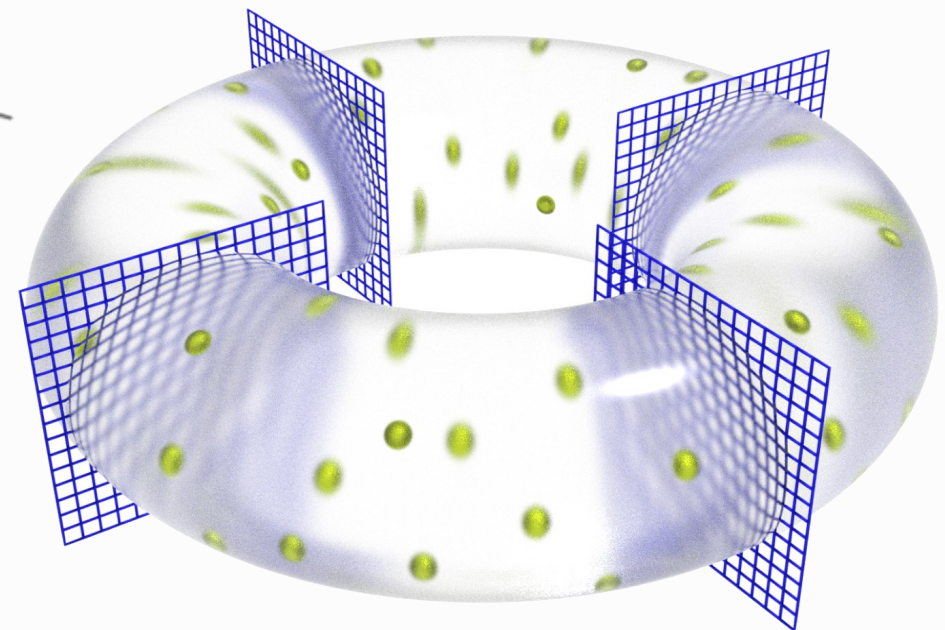
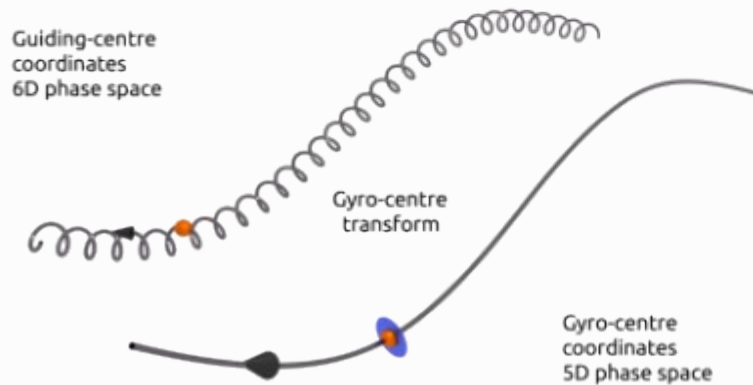


The Vlasov–Maxwell system of equations

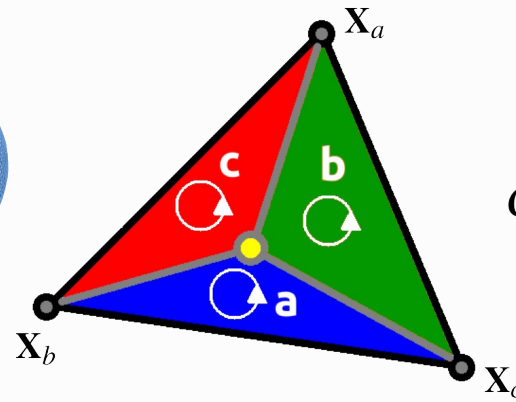
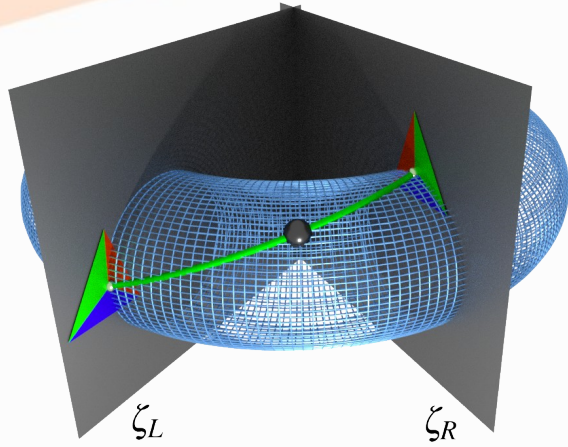
The gyro-averaged evolution of phase-space density in five-dimensional phase space of $(R, \zeta, Z, v_{\parallel}, \mu)$, where $\mu = mv_{\perp}^2/2B$ is the magnetic moment, and v_{\parallel} is the parallel velocity for the particle, is given by

$$\frac{d}{dt} f_i = \frac{\partial f_i}{\partial t} + \dot{\mathbf{X}} \cdot \nabla f_i + \dot{v}_{\parallel} \frac{\partial f_i}{\partial v_{\parallel}} = 0$$

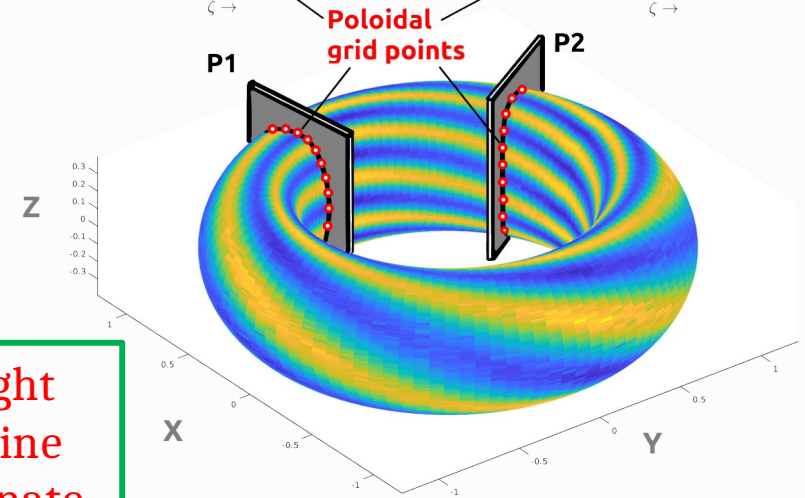
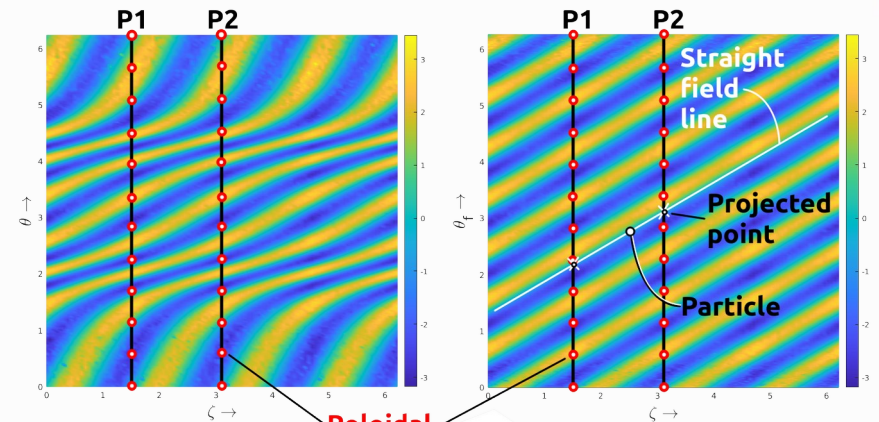
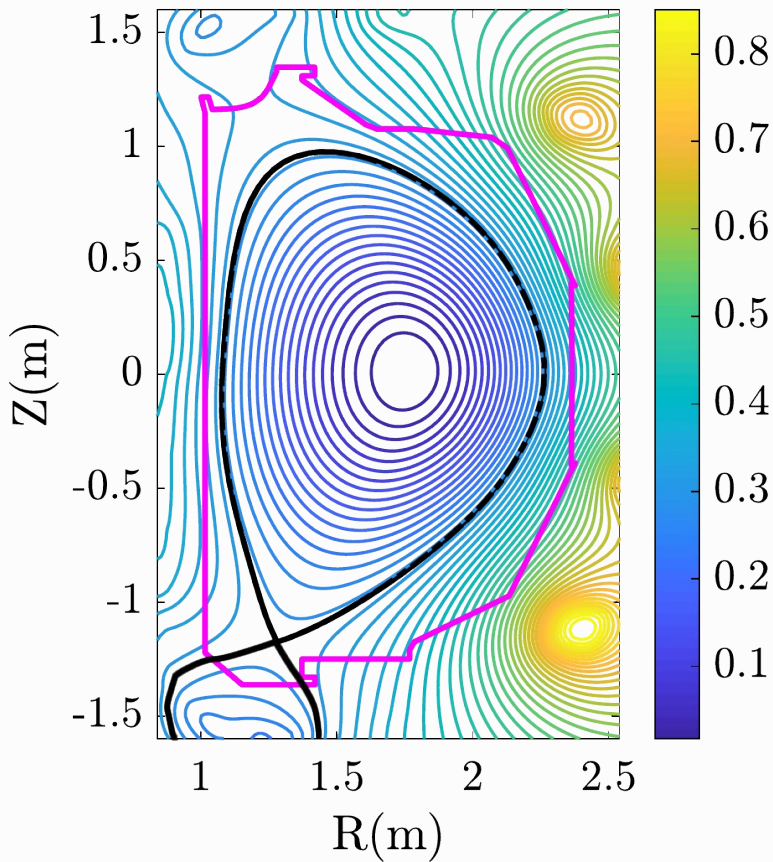
Particle-in-cell



Gather-Scatter operations for field and charges

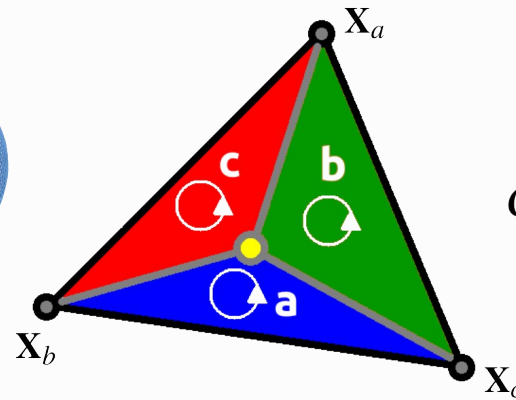
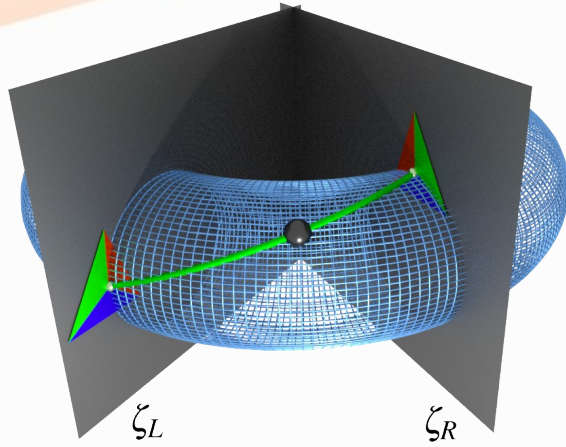


$$\phi(\mathbf{x}) = \left(\frac{a \phi_a + b \phi_b + c \phi_c}{a + b + c} \right)$$



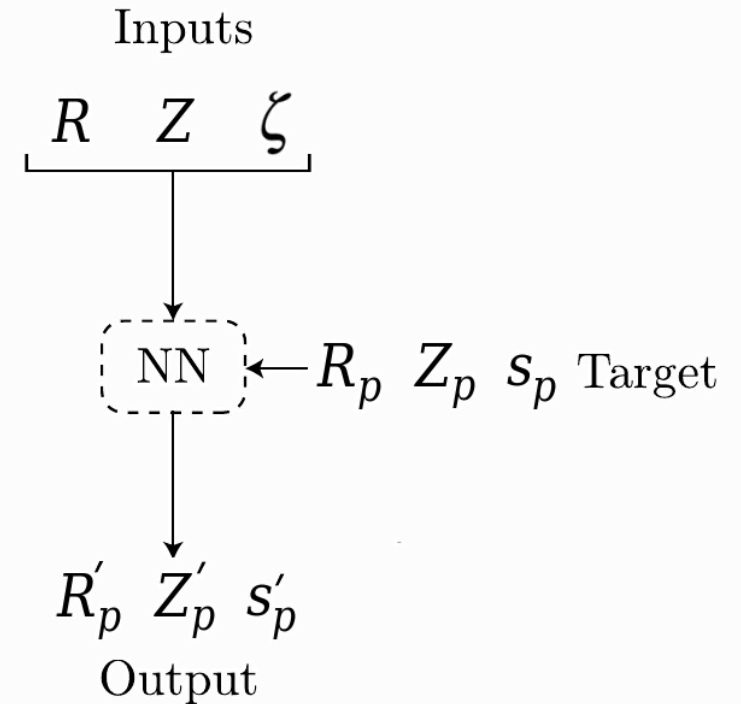
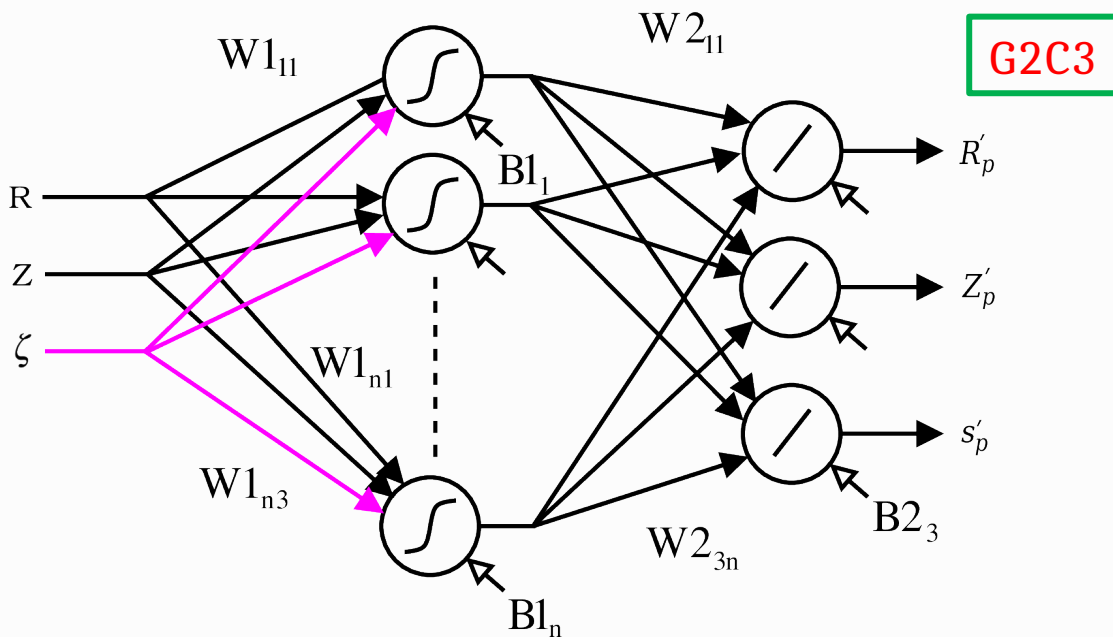
Straight field line coordinate

Gather-Scatter operations for field and charges



$$\phi(\mathbf{x}) = \left(\frac{a \phi_a + b \phi_b + c \phi_c}{a + b + c} \right)$$

Neural network as a universal approximator



Kolmogorov–Arnold representation theorem

In [real analysis](#) and [approximation theory](#), the Kolmogorov–Arnold representation theorem (or superposition theorem) states that every [multivariate continuous function](#) can be represented as a superposition of the two-argument addition and continuous functions of one variable. It solved a more constrained, yet more general form of [Hilbert's thirteenth problem](#).

The works of [Vladimir Arnold](#) and [Andrey Kolmogorov](#) established that if f is a multivariate continuous function, then f can be written as a finite [composition](#) of continuous functions of a single variable and the [binary operation](#) of [addition](#). More specifically,

$$f(\mathbf{x}) = f(x_1, \dots, x_n) = \sum_{q=0}^{2n} \Phi_q \left(\sum_{p=1}^n \phi_{q,p}(x_p) \right)$$

“Universal approximation theorems”

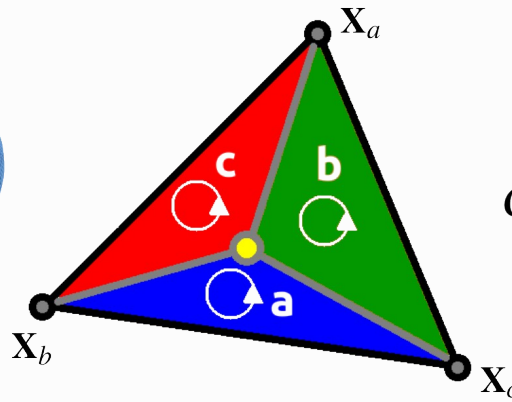
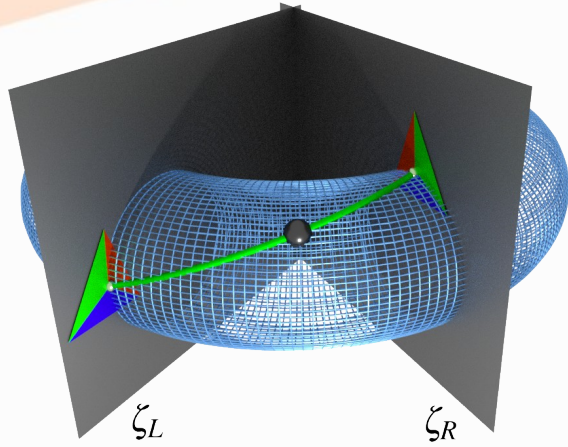


WIKIPEDIA
The Free Encyclopedia

[Andrey Kolmogorov](#), "On the representation of continuous functions of several variables by superpositions of continuous functions of a smaller number of variables", [Proceedings of the USSR Academy of Sciences](#), 108 (1956), pp. 179–182; English translation: Amer. Math. Soc. Transl., 17 (1961), pp. 369–373.

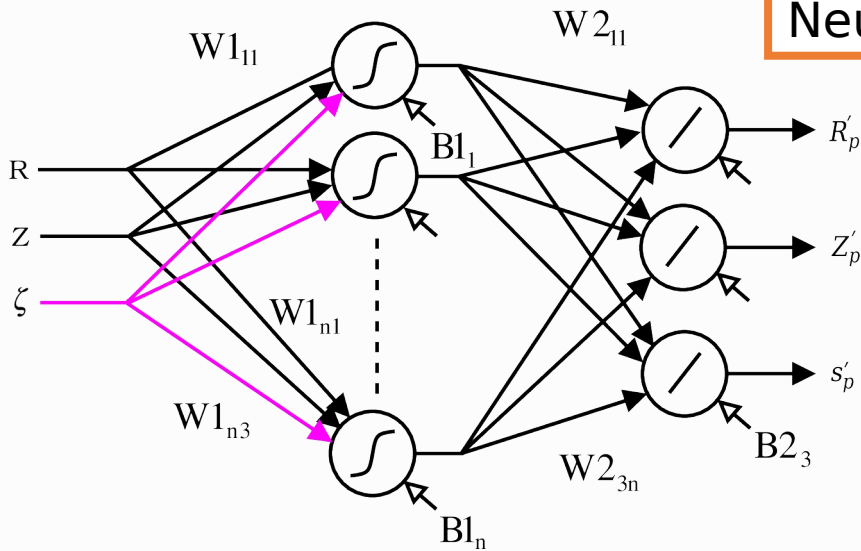
[Vladimir Arnold](#), "On functions of three variables", [Proceedings of the USSR Academy of Sciences](#), 114 (1957), pp. 679–681; English translation: Amer. Math. Soc. Transl., 28 (1963), pp. 51–54.

Gather-Scatter operations for field and charges

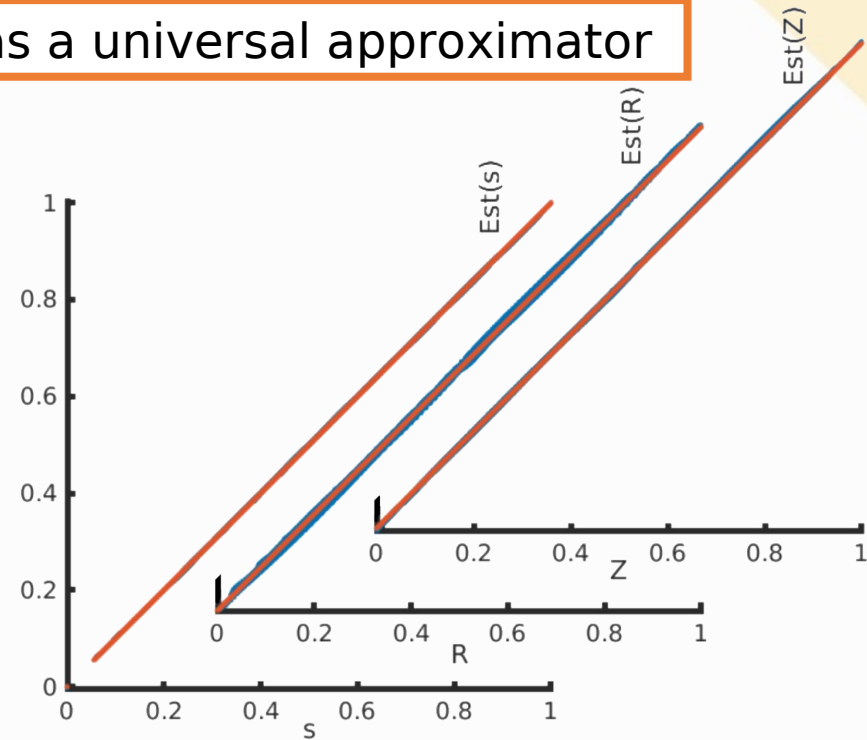


$$\phi(\mathbf{x}) = \left(\frac{a \phi_a + b \phi_b + c \phi_c}{a + b + c} \right)$$

Neural network as a universal approximator



G2C3



Estimation Error

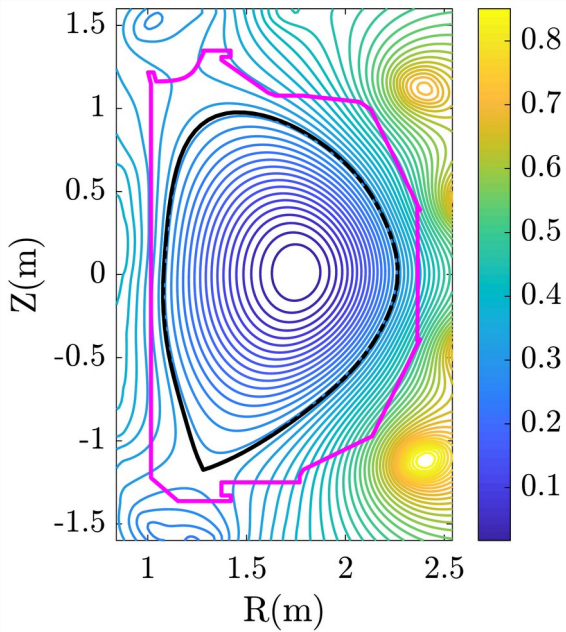
Comparison of the trained neural network output against the target values. Left lower panel shows the relation for δs , center panel for δR , and the right panel shows δZ . Notice that a error free map corresponds to a 45° straight line.

Benchmarking ITG mode in DIII-D [Shot # 158103]:

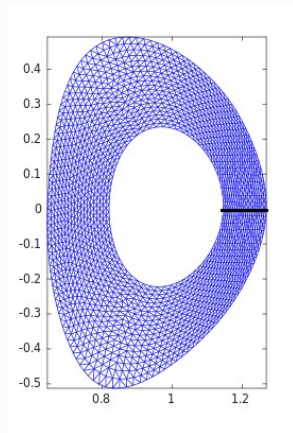
(Linear-, Adiabatic electron-, gyrokinetic ion-, Electrostatic- case)

Ion Temperature Gradient (ITG) mode

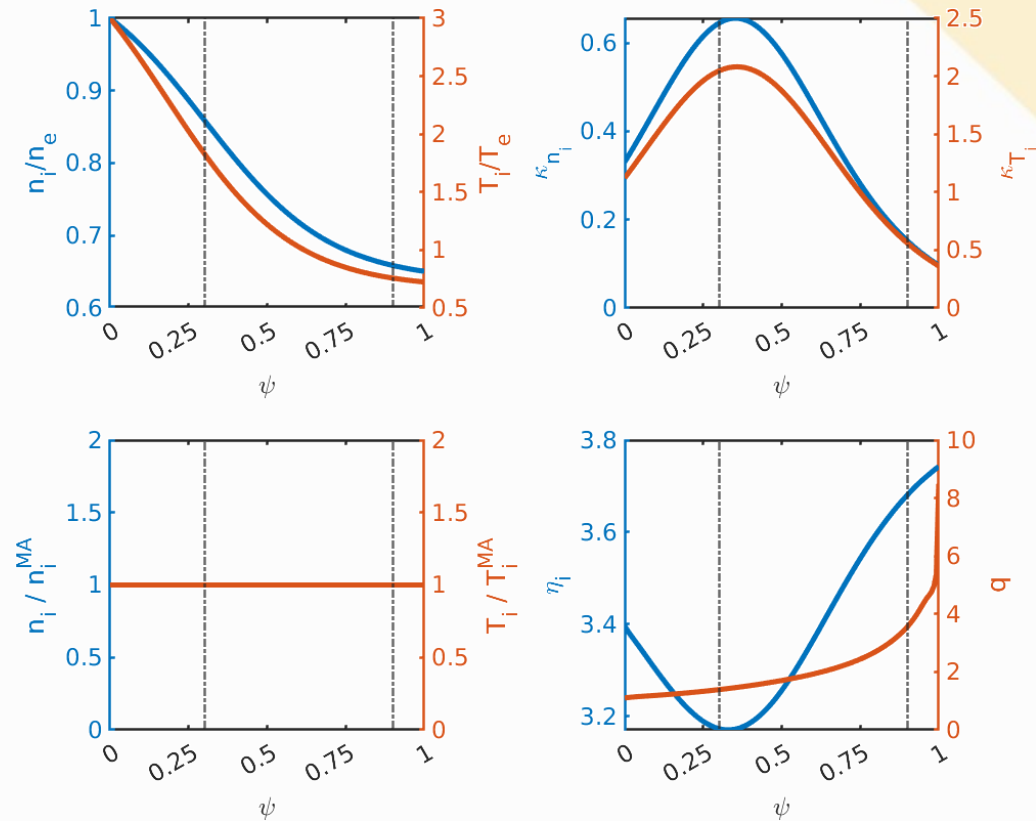
Flux function



Simulation grid

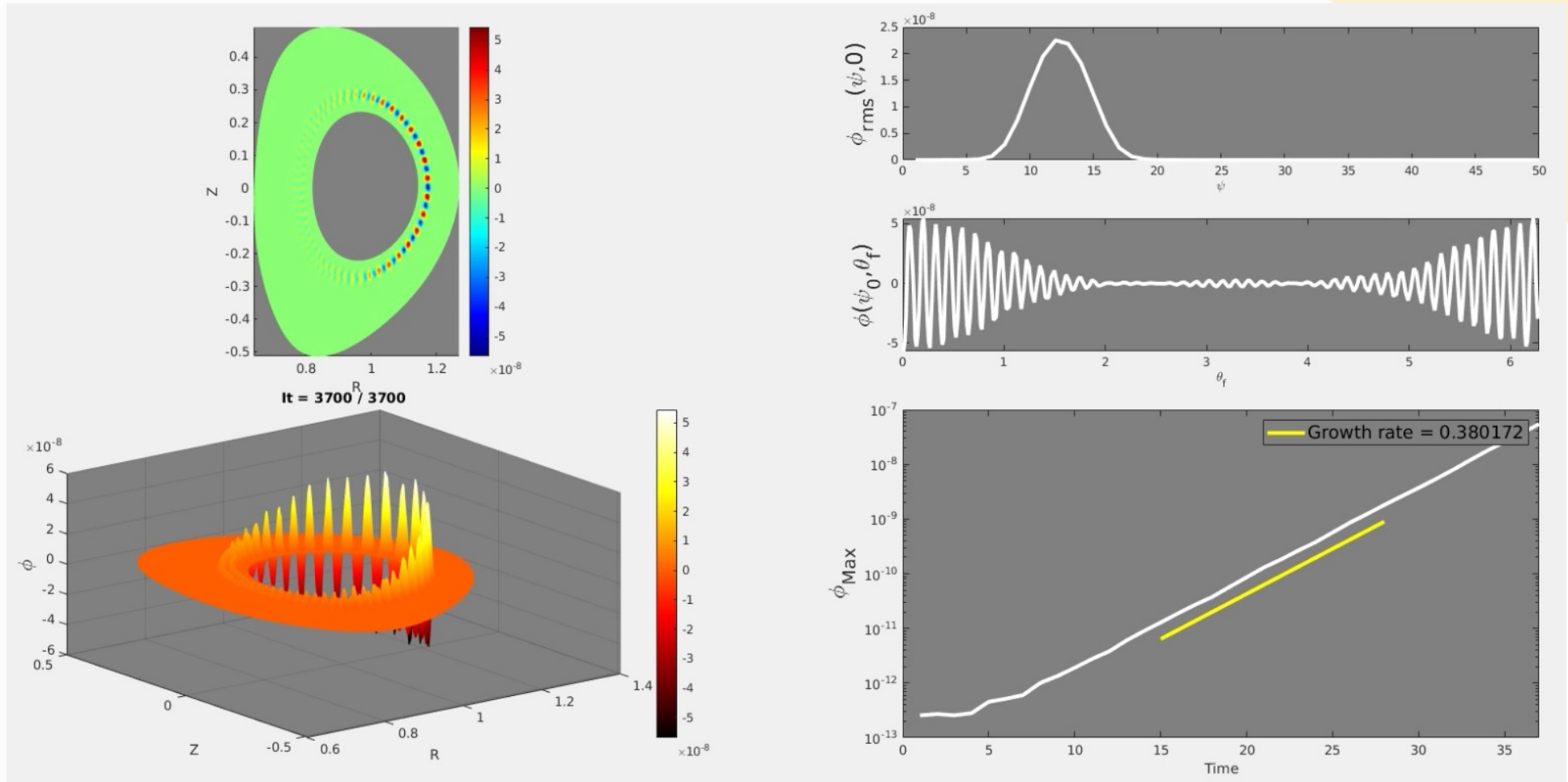


Temperature and density (cyclone) profiles:



Verification of Linear ITG mode in the core region of DIII-D tokamak

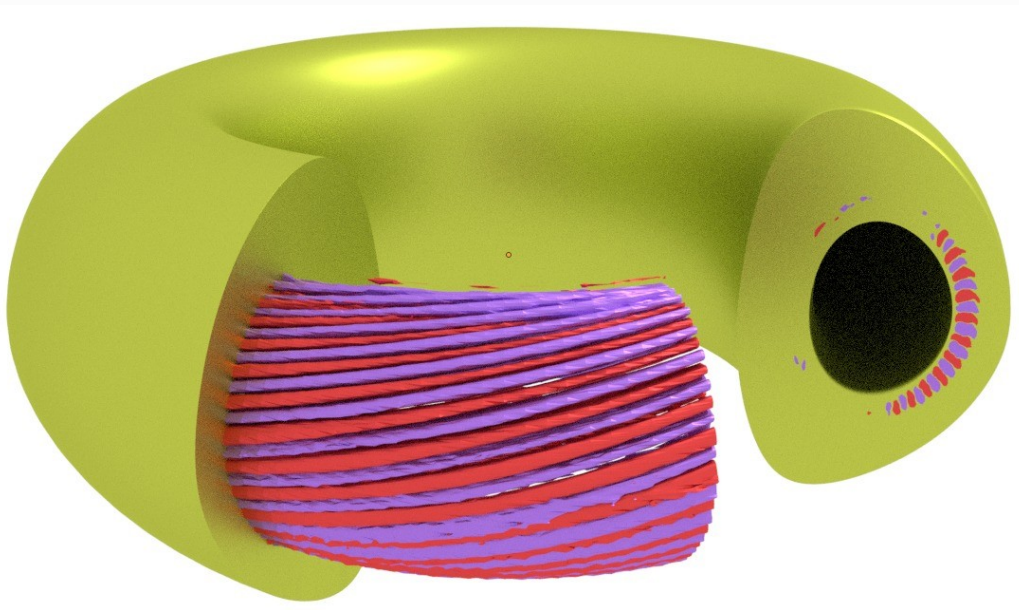
Electric
potential



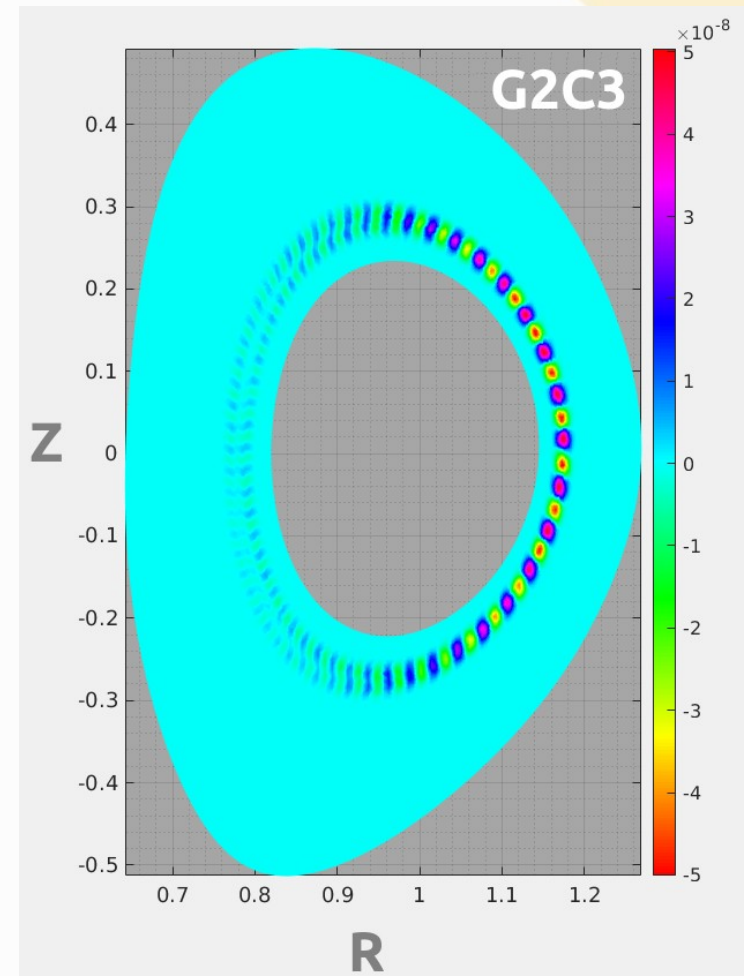
Verification of Linear ITG mode in the core region of DIII-D tokamak

Electric
potential

3D View

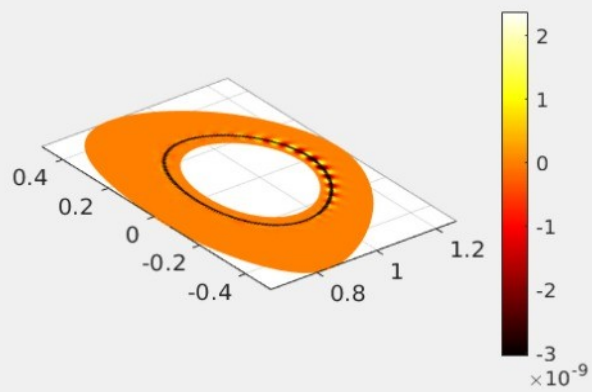


2D View

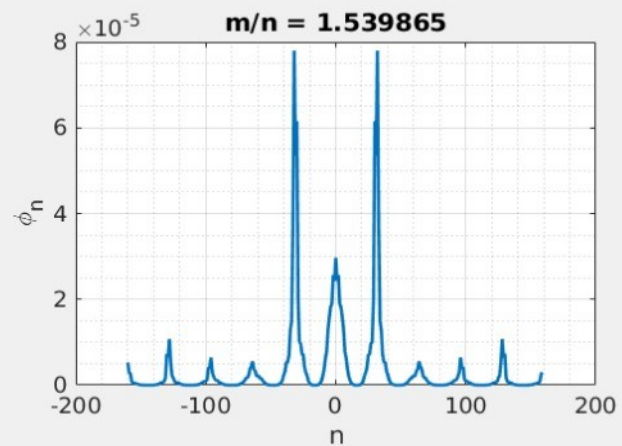
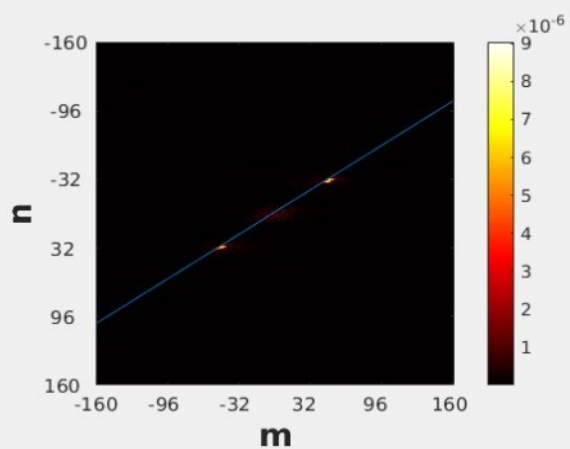
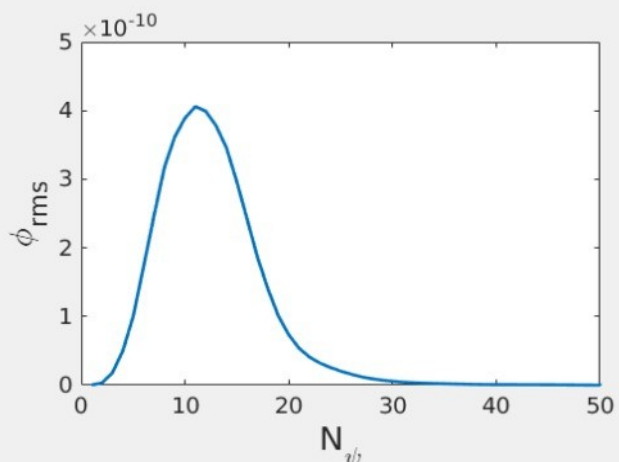
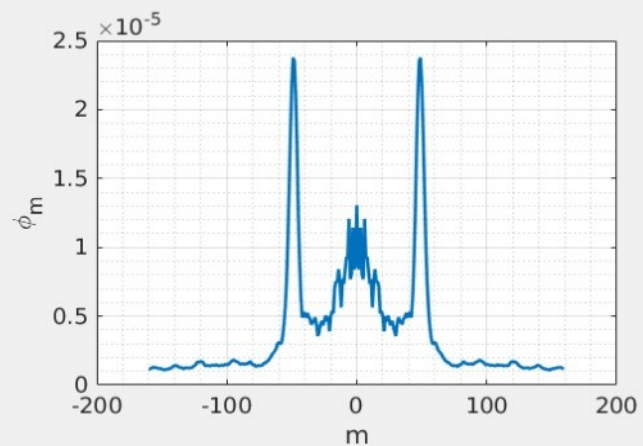
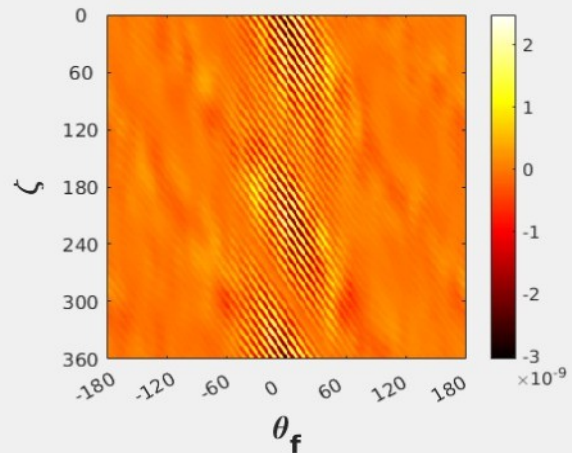


Mode Analysis

Electric
potential



Flux surface: 11/50



Capabilities of G2C3

□ G2C3 is a global code currently under development at IISc Bangalore.

The G2C3 code has the following features:

- ❖ G2C3 is a first principle particle-in-cell (PIC) code based on cylindrical coordinates
- ❖ Global approach for plasma and background magnetic geometry, obtained from axisymmetric ideal MHD equilibria computed with EFIT and IPREQ code.
- ❖ Both gyrokinetic (5D for low-frequency micro-turbulence) and fully kinetic (6D for high-frequency modes) particle integrators.
- ❖ Field-aligned particle grid interpolation for axisymmetric mesh in cylindrical coordinates.
- ❖ G2C3 has MPI parallelization with particle decomposition.
- ❖ Poisson solver using PETSc library.
- ❖ Neural Network for particle locating, gathering scattering operation.
- ❖ Microturbulence: Gyrokinetic thermal ion and adiabatic electron.



**Thank you
for your
attention.**